# Prediction of <br> Class and Property Assertions on OWL Ontologies through Evidence Combination 

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## Motivation

Semantic Web knowledge bases characterized by uncertainty

- incompleteness / inconsistency
- Purely dedutcive methods may fall short

Exploiting alternative (approximate / inductive) approaches to perform data mining tasks

## Proposed Approach

In particular: task of prediction of assertions

- class-membership
- object and data-type props filler

Proposal

- Nearest Neighbors approach
- Dempster-Shafer Evidence Theory (DST)
- BBA, Belief, Plausibility, Confirmation
- Evidence combination
- DS, Yager, other combination rules


## DL Knowledge Bases

Knowledge Base $\mathcal{K}=\langle\mathcal{T}, \mathcal{A}\rangle$

- TBox $\mathcal{T}$ : set of axioms defining concepts and properties
- ABox $\mathfrak{A}$ : set of assertions concerning the world-state
" Facts that involve the individuals (resources) using concepts and properties
- Reasoning services
- open-world semantics


## Dissimilarity Measures/1

- Given a context of concepts

$$
\mathrm{C}=\left\{C_{1}, C_{2}, \ldots, C_{\mathrm{m}}\right\}
$$

- Projection function:
$\forall a \in \operatorname{Ind}(\mathcal{A}) \quad \pi_{i}(a)= \begin{cases}1 & \mathcal{K} \models C_{i}(a) \\ 0 & \mathcal{K} \models \neg C_{i}(a) \\ \pi_{i} & \text { otherwise }\end{cases}$
- Discernibility function for $C_{i}$ :

$$
\delta_{i}(a, b)=\left|\pi_{i}(a)-\pi_{i}(b)\right|
$$

## Dissimilarity Measures/2

- Given a context $\mathrm{C}, \mathrm{p} \in \mathbf{R}$ and $w \in \mathbf{R}^{\mathrm{n}}$ family of dissimilarity measures:

$$
d_{p}^{C}(a, b)=\left[\sum_{C_{i} \in \mathrm{C}} w_{i} \delta_{i}(a, b)^{p}\right]^{\frac{1}{p}}
$$

## Evidence Theory

Frame of discernment $\Omega$

- set of hypotheses for a certain domain

Basic belief assignment (BBA) $m: 2^{\Omega} \rightarrow[0,1]$

- $\sum_{\mathrm{A}} m(A)=1$
- $m(A)$ belief committed exactly to $A$
- no additional claims about its subsets
- $m(A)>0=>A$ is a focal element


## Belief and Plausibility

- Belief function:

$$
\forall A \in 2^{\Omega} \quad \operatorname{Bel}(A)=\sum_{\emptyset \neq B \subseteq A} m(B) \in[0,1]
$$

- Plausibility function:

$$
\forall A \in 2^{\Omega} \quad P l(A)=\sum_{B \cap A \neq \emptyset} m(B) \in[0,1]
$$

## Rules of Combination

Given BBAs $m_{1}$ and $m_{2}$

- DS rule
$m_{12}(A)=\left(m_{1} \oplus m_{2}\right)(A)=\frac{\sum_{B \cap C=A} m_{1}(B) m_{2}(C)}{1-\sum_{B \cap C=\emptyset} m_{1}(B) m_{2}(C)}$
normalized version:
- 1-c hides the contrast between the BBAs


## Rules of Combination/2

- Yager's rule
$m_{12}(A)=\left\{\begin{array}{cl}\sum_{B \cap C=A} m_{1}(B) m_{2}(C) & A \neq \Omega \wedge A \neq \emptyset \\ m_{1}(\Omega) m_{2}(\Omega)+c & A=\Omega \\ 0 & A=\emptyset\end{array}\right.$
- more epistemologically sound: contrast attributed to the case $\mathrm{A}=\Omega$ (total ignorance)
- Other rules used in the experiments: Dubois-Pradé, Mixing


## Evidential Nearest-Neighbors

- Given
- A set of values $V$ (to be predicted)
- a training set of labeled individuals

$$
\operatorname{TrSet}=\left\{\left(x_{1}, v_{1}\right), \ldots,\left(x_{\mathrm{M}}, v_{\mathrm{M}}\right)\right\} \subseteq \operatorname{Ind}(\mathcal{A}) \times V
$$

- a query individual $x_{q}$
- Select the set of $k$ nearest neighbors $N_{\mathrm{k}}\left(x_{\mathrm{q}}\right)$ according to a (dis)similarity measure


## Evidential Nearest-Neighbors

- Each $\left(x_{i}, v_{\mathrm{i}}\right)$ in $N_{\mathrm{k}}\left(x_{\mathrm{q}}\right)$ induces a BBA $m_{i}$ regarding the value to be predicted for $x_{q}$
$m_{i}(A)= \begin{cases}\lambda \sigma\left(d\left(x_{q}, x_{i}\right)\right) & A=\left\{v_{i}\right\} \\ 1-\lambda \sigma\left(d\left(x_{q}, x_{i}\right)\right) & A=V \\ 0 & \text { otherwise }\end{cases}$
- Combine the induced BBAs:

$$
\bar{m}=\bigoplus_{j=1}^{k} m_{j}=m_{1} \oplus \cdots \oplus m_{k}
$$

## Evidential Nearest-Neighbors

- Predict based on belief / plausibility values:

$$
v_{q}=\underset{\left(x_{i}, v_{i}\right) \in N_{k}\left(x_{q}\right)}{\operatorname{argmax}} \overline{\operatorname{Bel}}\left(\left\{v_{i}\right\}\right)
$$

$$
v_{q}=\underset{\left(x_{i}, v_{i}\right) \in N_{k}\left(x_{q}\right)}{\operatorname{argmax}} \overline{P l}\left(\left\{v_{i}\right\}\right)
$$

## Evidential Nearest-Neighbors

- Alternatively, use a confirmation function

$$
C(A)=\operatorname{Bel}(A)+\operatorname{Pl}(A)-1
$$

then:

$$
v_{q}=\underset{\left(x_{i}, v_{i}\right) \in N_{k}\left(x_{q}\right)}{\operatorname{argmax}} \bar{C}\left(\left\{v_{i}\right\}\right)
$$

## Prediction Tasks

- Class-membership w.r.t. $Q$ :

$$
V_{Q}=\{-1,+1\} \quad \text { or } \quad V_{Q}=\{-1,0,+1\}
$$

- Object property $R$ filler:

$$
V_{R}=\operatorname{Ind}(\mathcal{A})
$$

- Datatype property $P$ value:

$$
V_{P}=\{v \mid \exists P(a, v) \in \mathcal{A}\}
$$

## Experiments

- Ontologies from standard repositories

| Ontology | $\begin{gathered} \mathrm{DL} \\ \text { language } \end{gathered}$ | \#concepts | \#object properties | \#datatype properties | \#individuals |
| :---: | :---: | :---: | :---: | :---: | :---: |
| FSM | $\mathcal{S O F}(\mathcal{D})$ | 20 | 10 | 7 | 37 |
| BCO | $\mathcal{A L C R O F}(\mathcal{D})$ | 196 | 22 | 3 | 112 |
| IMDB | $\mathcal{A L I N}(\mathcal{D})$ | 7 | 5 | 13 | 302 |
| BioPax | $\mathcal{A L C I F}(\mathcal{D})$ | 74 | 70 | 40 | 323 |
| HDis | $\mathcal{A L C I F}(\mathcal{D})$ | 1498 | 10 | 15 | 639 |

- 10 fold cross validation
- $k=\log \mid$ TSet $\mid$
- 4 combination rules
- Random classes created with $\mathfrak{A L C}$ ops
- 5 built-in functional properties


## Indices

Using a reasoner to decide the ground truth:

- Match rate
- Omission error rate
- Commission error rate
- Induction rate
(M\%)
(O\%)
(C\%)
(I\%)


## Outcomes

## Class Membership

| Ontology |  | Dempster | Dubois-Prade | Mixing | Yager |
| :---: | :---: | :---: | :---: | :---: | :---: |
| FSM | M\% | $86.60 \pm 04.42$ | $84.75 \pm 04.49$ | $85.80 \pm 03.90$ | $89.00 \pm 04.65$ |
|  | C\% | $04.69 \pm 03.05$ | $06.65 \pm 03.06$ | $05.49 \pm 02.33$ | $02.29 \pm 02.76$ |
|  | O\% | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ |
|  | I\% | $08.71 \pm 00.29$ | $08.71 \pm 00.29$ | $08.71 \pm 00.29$ | $08.71 \pm 00.29$ |
| BioPax | M\% | $94.93 \pm 00.32$ | $94.76 \pm 00.32$ | $94.93 \pm 00.32$ | $94.93 \pm 00.32$ |
|  | C\% | $00.15 \pm 00.00$ | $00.32 \pm 00.00$ | $00.15 \pm 00.00$ | $00.15 \pm 00.00$ |
|  | O\% | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ |
|  | I\% | $04.91 \pm 00.29$ | $04.91 \pm 00.29$ | $04.91 \pm 00.29$ | $04.91 \pm 00.29$ |
| BCO | M\% | $85.21 \pm 04.04$ | $84.54 \pm 04.83$ | $85.21 \pm 04.04$ | $85.45 \pm 04.18$ |
|  | C\% | $00.81 \pm 00.56$ | $01.47 \pm 01.54$ | $00.81 \pm 00.56$ | $00.57 \pm 00.70$ |
|  | O\% | $00.05 \pm 00.14$ | $00.14 \pm 00.23$ | $00.05 \pm 00.14$ | $00.05 \pm 00.14$ |
|  | I\% | $13.93 \pm 03.72$ | $13.95 \pm 03.64$ | $13.93 \pm 03.72$ | $13.93 \pm 03.72$ |

# Outcomes Object Property Values 

| Ontology |  | Dempster | Dubois-Prade | Mixing | Yager |
| :---: | ---: | ---: | ---: | ---: | ---: |
| FSM | M\% | $99.64 \pm 00.33$ | $99.64 \pm 00.33$ | $99.98 \pm 00.07$ | $99.64 \pm 00.33$ |
|  | $\mathrm{C} \%$ | $00.02 \pm 00.07$ | $00.36 \pm 00.33$ | $00.02 \pm 00.07$ | $00.36 \pm 00.33$ |
|  | $\mathrm{O} \%$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ |
|  | $\mathrm{I} \%$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ |
|  | $\mathrm{M} \%$ | $100.00 \pm 00.00$ | $100.00 \pm 00.00$ | $100.00 \pm 00.00$ | $100.00 \pm 00.00$ |
|  | $\mathrm{C} \%$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ |
|  | $\mathrm{O} \%$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ |
|  | $\mathrm{I} \%$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ |
| BCO | $\mathrm{M} \%$ | $100.00 \pm 00.00$ | $100.00 \pm 00.00$ | $100.00 \pm 00.00$ | $100.00 \pm 00.00$ |
|  | $\mathrm{C} \%$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ |
|  | $\mathrm{O} \%$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ |
|  | $\mathrm{I} \%$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ |

# Outcomes Data Property Values 

| Ontology |  | Dempster | Dubois-Prade | Mixing | Yager |
| :---: | ---: | ---: | ---: | ---: | ---: |
| BCO | $\mathrm{M} \%$ | $64.15 \pm 13.53$ | $33.79 \pm 11.64$ | $63.52 \pm 15.08$ | $71.14 \pm 10.00$ |
|  | $\mathrm{C} \%$ | $35.85 \pm 13.53$ | $13.61 \pm 10.52$ | $36.48 \pm 15.08$ | $28.86 \pm 10.00$ |
|  | $\mathrm{O} \%$ | $00.00 \pm 00.00$ | $52.60 \pm 15.95$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ |
|  | $\mathrm{I} \%$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ |
|  | $\mathrm{M} \%$ | $65.60 \pm 06.38$ | $39.73 \pm 14.19$ | $66.25 \pm 05.94$ | $61.34 \pm 08.28$ |
|  | $\mathrm{C} \%$ | $30.74 \pm 06.57$ | $13.62 \pm 10.52$ | $30.09 \pm 06.13$ | $35.00 \pm 09.78$ |
|  | $\mathrm{O} \%$ | $03.66 \pm 03.74$ | $43.01 \pm 19.99$ | $03.66 \pm 03.74$ | $03.66 \pm 03.74$ |
|  | $\mathrm{I} \%$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ |
|  | $\mathrm{M} \%$ | $61.00 \pm 19.15$ | $61.00 \pm 19.15$ | $61.00 \pm 19.15$ | $61.00 \pm 19.15$ |
|  | $\mathrm{C} \%$ | $35.62 \pm 17.32$ | $35.62 \pm 17.32$ | $35.62 \pm 17.32$ | $35.62 \pm 17.32$ |
|  | $\mathrm{O} \%$ | $03.38 \pm 04.94$ | $03.38 \pm 04.94$ | $03.38 \pm 04.94$ | $03.38 \pm 04.94$ |
|  | $\mathrm{I} \%$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ | $00.00 \pm 00.00$ |

## Conclusions

## Contribution

- Evidential NN procedure based on
- DST
- Dissim. measure
- Prediction of
- class-membership
- (functional) role fillers


## Outlook

- Tackle prediction of non-functional properties vals
- Regression/Ranking
- based on nonexplicit criteria
- Integration with Rough DL


## The End

## Thank you

## Questions?

Offline
Find us at: http://lacam.di.uniba.it:8000/

