

Logical Structure Analysis of Scientific Publications in Mathematics

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Overview



- ▶ LOD Cloud has been growing at 200-300% per year since 2007*
- ▶ Prevalent domains: **government** (43%), **geographic** (22%) and **life sciences** (9%)
- ▶ However, it lacks data sets related to **academic mathematics**

* C.Bizer et al. State of the Web of Data.
LDOW WWW'11



- ① Background
- ② Proposed Semantic Model
- ③ Analysis Methods
- ④ Experiments and Evaluation
- ⑤ Prototype



Mathematical Scholarly Papers

Essential features

- ▶ Well-structured documents
- ▶ The presence of mathematical formulae
- ▶ Peculiar vocabulary ("*mathematical vernacular*")



Research Objectives

Current study

- ▶ Specification of the document logical structure
- ▶ Methods for extracting structural elements

Long-term goals

- ▶ A large corpus of semantically annotated papers
- ▶ Semantic search of mathematical papers



Modelling the Structure of Scientific Publications

ABCDE format

- ▶ LaTeX-based format to represent the narrative structure of proceedings and workshop contributions
- ▶ Sections:
 - **A**nnotations (Dublin Core metadata)
 - **B**ackground (e.g. description of research positioning)
 - **C**ontribution (description of the presented work)
 - **D**iscussion (e.g. comparison with other work)
 - **E**ntities (citations)



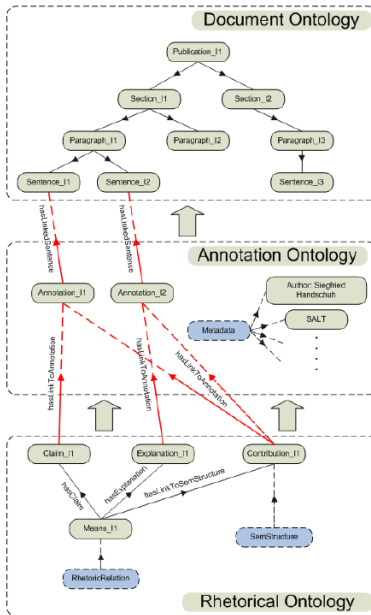
Modelling the Structure of Scientific Publications

SALT

- ▶ LaTeX-based authoring tool for generating semantically annotated PDF documents
- ▶ Three ontologies:
 - SALT Document Ontology
 - SALT Annotation Ontology
 - SALT Rhetorical Ontology



SALT Layers

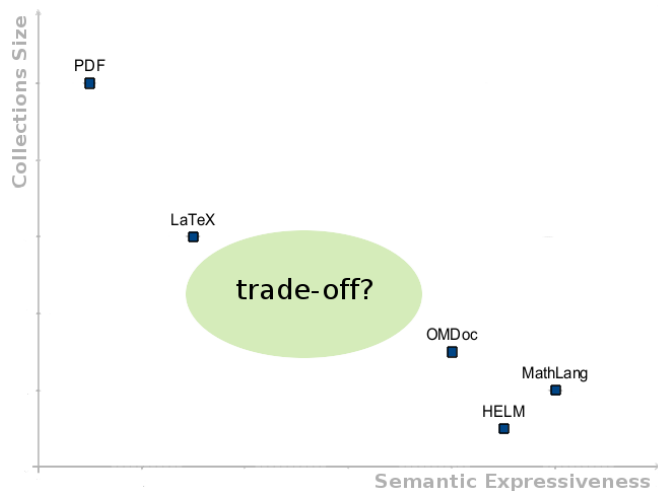


Mathematical Knowledge Representation

- ▶ Languages for formalized mathematics
 - Mizar
 - Coq
 - Isabelle
- ▶ Semiformal math languages
 - HELM ontology
 - MathLang
 - OMDoc format (+ OMDoc ontology, sTeX)
- ▶ Presentation/authoring formats
 - PDF
 - \LaTeX



Mathematical Knowledge Representation



Trade-off Candidates

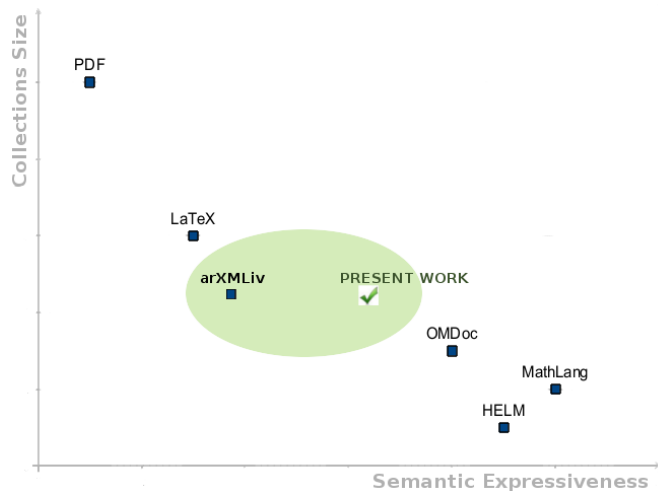
- ▶ arXMLiv format
 - XHTML+MathML
 - Marked up theorem-like elements, sections, equations
 - Automatic conversion for LaTeX documents with styles of available bindings (LaTeXML)
 - 60% of arXiv.org were converted into the format
- ▶ Present work
 - Follow the slides ⇒



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Mathematical Knowledge Representation



Proposed Semantic Model

- ▶ It is an **ontology** that captures the structural layout of mathematical scholarly papers (as in the LaTeX markup)
- ▶ The **segment** represents the finest level of granularity and has the properties:
 - starting and ending positions
 - the text or math contents
 - functional role
- ▶ Select **most frequent segments** from sample collections of genuine papers
- ▶ Consider synonyms as one concept (e.g. *conjecture* and *hypothesis*)



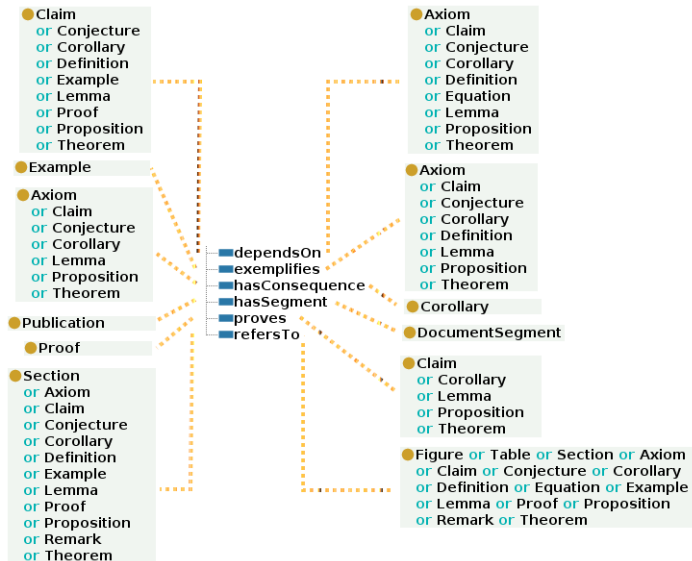
Proposed Semantic Model (cont.)

- ▶ Select **basic semantic relations** between segments from the prior-art models
- ▶ Integration with SALT Document Ontology classes:
 - Publication
 - Section
 - Figure
 - Table



Ontology Elements

<http://c1l.niimm.ksu.ru/ontologies/mocassin#>



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Logical Structure Analysis

- ▶ The ontology specifies a controlled vocabulary to **semantic analysis**
- ▶ Two analysis tasks:
 - recognizing the types of document segments
 - recognizing the semantic relations between them



Example

1. A CONSEQUENCE OF THE HYPERBOLIC COSINE DEFINITION

THEOREM 1.1. The Bessel function J_0 is bounded by the absolute value of the modified Bessel function I_0 . In other words, if x is a real number, then

$$|J_0(x)| \leq I_0(x)$$

for all $x \in \mathbb{R}$.

PROOF. We begin by recalling that $J_0(x) = \sum_{k=0}^{\infty} \frac{(-1)^k}{k! \Gamma(k+1)} \left(\frac{x}{2}\right)^{2k}$ and $I_0(x) = \sum_{k=0}^{\infty} \frac{1}{k! \Gamma(k+1)} \left(\frac{x}{2}\right)^{2k}$. Since $|(-1)^k| \leq 1$, we have $|J_0(x)| \leq \sum_{k=0}^{\infty} \frac{1}{k! \Gamma(k+1)} \left(\frac{x}{2}\right)^{2k} = I_0(x)$.

2. A CONSEQUENCE OF THE HYPERBOLIC COSINE DEFINITION

THEOREM 1.2. The Bessel function J_0 is bounded by the absolute value of the modified Bessel function I_0 . In other words, if x is a real number, then

$$|J_0(x)| \leq I_0(x)$$

for all $x \in \mathbb{R}$.

PROOF. We begin by recalling that $J_0(x) = \sum_{k=0}^{\infty} \frac{(-1)^k}{k! \Gamma(k+1)} \left(\frac{x}{2}\right)^{2k}$ and $I_0(x) = \sum_{k=0}^{\infty} \frac{1}{k! \Gamma(k+1)} \left(\frac{x}{2}\right)^{2k}$. Since $|(-1)^k| \leq 1$, we have $|J_0(x)| \leq \sum_{k=0}^{\infty} \frac{1}{k! \Gamma(k+1)} \left(\frac{x}{2}\right)^{2k} = I_0(x)$.

3. A CONSEQUENCE OF THE HYPERBOLIC COSINE DEFINITION

THEOREM 1.3. The Bessel function J_0 is bounded by the absolute value of the modified Bessel function I_0 . In other words, if x is a real number, then

$$|J_0(x)| \leq I_0(x)$$

for all $x \in \mathbb{R}$.

PROOF. We begin by recalling that $J_0(x) = \sum_{k=0}^{\infty} \frac{(-1)^k}{k! \Gamma(k+1)} \left(\frac{x}{2}\right)^{2k}$ and $I_0(x) = \sum_{k=0}^{\infty} \frac{1}{k! \Gamma(k+1)} \left(\frac{x}{2}\right)^{2k}$. Since $|(-1)^k| \leq 1$, we have $|J_0(x)| \leq \sum_{k=0}^{\infty} \frac{1}{k! \Gamma(k+1)} \left(\frac{x}{2}\right)^{2k} = I_0(x)$.

4. A CONSEQUENCE OF THE HYPERBOLIC COSINE DEFINITION

THEOREM 1.4. The Bessel function J_0 is bounded by the absolute value of the modified Bessel function I_0 . In other words, if x is a real number, then

$$|J_0(x)| \leq I_0(x)$$

for all $x \in \mathbb{R}$.

PROOF. We begin by recalling that $J_0(x) = \sum_{k=0}^{\infty} \frac{(-1)^k}{k! \Gamma(k+1)} \left(\frac{x}{2}\right)^{2k}$ and $I_0(x) = \sum_{k=0}^{\infty} \frac{1}{k! \Gamma(k+1)} \left(\frac{x}{2}\right)^{2k}$. Since $|(-1)^k| \leq 1$, we have $|J_0(x)| \leq \sum_{k=0}^{\infty} \frac{1}{k! \Gamma(k+1)} \left(\frac{x}{2}\right)^{2k} = I_0(x)$.

5. A CONSEQUENCE OF THE HYPERBOLIC COSINE DEFINITION

THEOREM 1.5. The Bessel function J_0 is bounded by the absolute value of the modified Bessel function I_0 . In other words, if x is a real number, then

$$|J_0(x)| \leq I_0(x)$$

for all $x \in \mathbb{R}$.

PROOF. We begin by recalling that $J_0(x) = \sum_{k=0}^{\infty} \frac{(-1)^k}{k! \Gamma(k+1)} \left(\frac{x}{2}\right)^{2k}$ and $I_0(x) = \sum_{k=0}^{\infty} \frac{1}{k! \Gamma(k+1)} \left(\frac{x}{2}\right)^{2k}$. Since $|(-1)^k| \leq 1$, we have $|J_0(x)| \leq \sum_{k=0}^{\infty} \frac{1}{k! \Gamma(k+1)} \left(\frac{x}{2}\right)^{2k} = I_0(x)$.

6. A CONSEQUENCE OF THE HYPERBOLIC COSINE DEFINITION

THEOREM 1.6. The Bessel function J_0 is bounded by the absolute value of the modified Bessel function I_0 . In other words, if x is a real number, then

$$|J_0(x)| \leq I_0(x)$$

for all $x \in \mathbb{R}$.

PROOF. We begin by recalling that $J_0(x) = \sum_{k=0}^{\infty} \frac{(-1)^k}{k! \Gamma(k+1)} \left(\frac{x}{2}\right)^{2k}$ and $I_0(x) = \sum_{k=0}^{\infty} \frac{1}{k! \Gamma(k+1)} \left(\frac{x}{2}\right)^{2k}$. Since $|(-1)^k| \leq 1$, we have $|J_0(x)| \leq \sum_{k=0}^{\infty} \frac{1}{k! \Gamma(k+1)} \left(\frac{x}{2}\right)^{2k} = I_0(x)$.

7. A CONSEQUENCE OF THE HYPERBOLIC COSINE DEFINITION

THEOREM 1.7. The Bessel function J_0 is bounded by the absolute value of the modified Bessel function I_0 . In other words, if x is a real number, then

$$|J_0(x)| \leq I_0(x)$$

for all $x \in \mathbb{R}$.

PROOF. We begin by recalling that $J_0(x) = \sum_{k=0}^{\infty} \frac{(-1)^k}{k! \Gamma(k+1)} \left(\frac{x}{2}\right)^{2k}$ and $I_0(x) = \sum_{k=0}^{\infty} \frac{1}{k! \Gamma(k+1)} \left(\frac{x}{2}\right)^{2k}$. Since $|(-1)^k| \leq 1$, we have $|J_0(x)| \leq \sum_{k=0}^{\infty} \frac{1}{k! \Gamma(k+1)} \left(\frac{x}{2}\right)^{2k} = I_0(x)$.

8. A CONSEQUENCE OF THE HYPERBOLIC COSINE DEFINITION

THEOREM 1.8. The Bessel function J_0 is bounded by the absolute value of the modified Bessel function I_0 . In other words, if x is a real number, then

$$|J_0(x)| \leq I_0(x)$$

for all $x \in \mathbb{R}$.

PROOF. We begin by recalling that $J_0(x) = \sum_{k=0}^{\infty} \frac{(-1)^k}{k! \Gamma(k+1)} \left(\frac{x}{2}\right)^{2k}$ and $I_0(x) = \sum_{k=0}^{\infty} \frac{1}{k! \Gamma(k+1)} \left(\frac{x}{2}\right)^{2k}$. Since $|(-1)^k| \leq 1$, we have $|J_0(x)| \leq \sum_{k=0}^{\infty} \frac{1}{k! \Gamma(k+1)} \left(\frac{x}{2}\right)^{2k} = I_0(x)$.



Example (cont.)

A FUNDAMENTAL PROPERTY OF THE RIEMANN INTEGRAL
DEFINITION 1.1. Let f be a function on the interval $[a, b]$. We say that f is Riemann integrable on $[a, b]$ if there exists a real number I such that for every $\epsilon > 0$ there exists a partition P_ϵ of $[a, b]$ such that for every refinement P of P_ϵ we have $|U(P, f) - I| < \epsilon$ and $|L(P, f) - I| < \epsilon$.

THEOREM 1.1. Let f be a function on the interval $[a, b]$. Then f is Riemann integrable on $[a, b]$ if and only if f is continuous on $[a, b]$.

1 **THEOREM 1.1.** Let f be a function on the interval $[a, b]$. Then f is Riemann integrable on $[a, b]$ if and only if f is continuous on $[a, b]$.

PROOF. Suppose f is continuous on $[a, b]$. Let $\epsilon > 0$. By the Heine-Borel theorem, the set $[a, b]$ is compact. For each $x \in [a, b]$, there exists a $\delta_x > 0$ such that $|f(t) - f(x)| < \epsilon/3$ for all $t \in [x - \delta_x, x + \delta_x] \cap [a, b]$. The collection of these intervals covers $[a, b]$. By compactness, there is a finite subcollection that covers $[a, b]$. Let P_ϵ be the partition consisting of the endpoints of these intervals. Then for any refinement P of P_ϵ , we have $|U(P, f) - L(P, f)| < \epsilon$.

2 **THEOREM 1.1.** Let f be a function on the interval $[a, b]$. Then f is Riemann integrable on $[a, b]$ if and only if f is continuous on $[a, b]$.

PROOF. Suppose f is Riemann integrable on $[a, b]$. Let $\epsilon > 0$. Then there exists a partition P_ϵ such that $|U(P_\epsilon, f) - L(P_\epsilon, f)| < \epsilon$. Let $x \in [a, b]$. If f is not continuous at x , then there exists a $\delta > 0$ such that for any δ , there are points $t, s \in [x - \delta, x + \delta] \cap [a, b]$ with $|f(t) - f(s)| \geq \epsilon/3$. This contradicts the integrability of f .

3 **THEOREM 1.1.** Let f be a function on the interval $[a, b]$. Then f is Riemann integrable on $[a, b]$ if and only if f is continuous on $[a, b]$.

PROOF. Suppose f is continuous on $[a, b]$. Let $\epsilon > 0$. By the Heine-Borel theorem, the set $[a, b]$ is compact. For each $x \in [a, b]$, there exists a $\delta_x > 0$ such that $|f(t) - f(x)| < \epsilon/3$ for all $t \in [x - \delta_x, x + \delta_x] \cap [a, b]$. The collection of these intervals covers $[a, b]$. By compactness, there is a finite subcollection that covers $[a, b]$. Let P_ϵ be the partition consisting of the endpoints of these intervals. Then for any refinement P of P_ϵ , we have $|U(P, f) - L(P, f)| < \epsilon$.

4 **THEOREM 1.1.** Let f be a function on the interval $[a, b]$. Then f is Riemann integrable on $[a, b]$ if and only if f is continuous on $[a, b]$.

PROOF. Suppose f is continuous on $[a, b]$. Let $\epsilon > 0$. By the Heine-Borel theorem, the set $[a, b]$ is compact. For each $x \in [a, b]$, there exists a $\delta_x > 0$ such that $|f(t) - f(x)| < \epsilon/3$ for all $t \in [x - \delta_x, x + \delta_x] \cap [a, b]$. The collection of these intervals covers $[a, b]$. By compactness, there is a finite subcollection that covers $[a, b]$. Let P_ϵ be the partition consisting of the endpoints of these intervals. Then for any refinement P of P_ϵ , we have $|U(P, f) - L(P, f)| < \epsilon$.

5 **THEOREM 1.1.** Let f be a function on the interval $[a, b]$. Then f is Riemann integrable on $[a, b]$ if and only if f is continuous on $[a, b]$.

PROOF. Suppose f is Riemann integrable on $[a, b]$. Let $\epsilon > 0$. Then there exists a partition P_ϵ such that $|U(P_\epsilon, f) - L(P_\epsilon, f)| < \epsilon$. Let $x \in [a, b]$. If f is not continuous at x , then there exists a $\delta > 0$ such that for any δ , there are points $t, s \in [x - \delta, x + \delta] \cap [a, b]$ with $|f(t) - f(s)| \geq \epsilon/3$. This contradicts the integrability of f .

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PROOF. Suppose f is continuous on $[a, b]$. Let $\epsilon > 0$. By the Heine-Borel theorem, the set $[a, b]$ is compact. For each $x \in [a, b]$, there exists a $\delta_x > 0$ such that $|f(t) - f(x)| < \epsilon/3$ for all $t \in [x - \delta_x, x + \delta_x] \cap [a, b]$. The collection of these intervals covers $[a, b]$. By compactness, there is a finite subcollection that covers $[a, b]$. Let P_ϵ be the partition consisting of the endpoints of these intervals. Then for any refinement P of P_ϵ , we have $|U(P, f) - L(P, f)| < \epsilon$.

7 **THEOREM 1.1.** Let f be a function on the interval $[a, b]$. Then f is Riemann integrable on $[a, b]$ if and only if f is continuous on $[a, b]$.

PROOF. Suppose f is Riemann integrable on $[a, b]$. Let $\epsilon > 0$. Then there exists a partition P_ϵ such that $|U(P_\epsilon, f) - L(P_\epsilon, f)| < \epsilon$. Let $x \in [a, b]$. If f is not continuous at x , then there exists a $\delta > 0$ such that for any δ , there are points $t, s \in [x - \delta, x + \delta] \cap [a, b]$ with $|f(t) - f(s)| \geq \epsilon/3$. This contradicts the integrability of f .



Example (cont.)

<p>A FUNDAMENTAL PROPERTY OF THE STRONG BROWNIAN MOTION</p> <p>THEOREM 1.1. Let $\{B_t\}_{t \geq 0}$ be a standard Brownian motion. Then for any $s > 0$ and $t > s$, the process $\{B_{t+s} - B_s\}_{t \geq 0}$ is a standard Brownian motion independent of \mathcal{F}_s.</p>	<p>1 THEOREM 1.1. Let $\{B_t\}_{t \geq 0}$ be a standard Brownian motion. Then for any $s > 0$ and $t > s$, the process $\{B_{t+s} - B_s\}_{t \geq 0}$ is a standard Brownian motion independent of \mathcal{F}_s.</p>	<p>2 THEOREM 1.1. Let $\{B_t\}_{t \geq 0}$ be a standard Brownian motion. Then for any $s > 0$ and $t > s$, the process $\{B_{t+s} - B_s\}_{t \geq 0}$ is a standard Brownian motion independent of \mathcal{F}_s.</p>	<p>4 THEOREM 1.1. Let $\{B_t\}_{t \geq 0}$ be a standard Brownian motion. Then for any $s > 0$ and $t > s$, the process $\{B_{t+s} - B_s\}_{t \geq 0}$ is a standard Brownian motion independent of \mathcal{F}_s.</p> <p>5 THEOREM 1.1. Let $\{B_t\}_{t \geq 0}$ be a standard Brownian motion. Then for any $s > 0$ and $t > s$, the process $\{B_{t+s} - B_s\}_{t \geq 0}$ is a standard Brownian motion independent of \mathcal{F}_s.</p>
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Recognizing the Types of Document Segments

We exploit the LaTeX markup extensively

- 1 Elicit a LaTeX environment
- 2 Associate it with a **string** that may be **either** the environment name **or** the environment title (if available)
- 3 Filter out standard formatting environments (e.g. *center*, *align*, *itemize*)
- 4 Compute **string similarity** between a string and canonical names of ontology concepts
- 5 Check if the found **most similar concept** is appropriate using a **predefined threshold**



Recognizing Navigational Relations

The *dependsOn* and *refersTo* relations are **navigational**

Assumption

Navigational relations are induced by **referential sentences**

Examples

- ▶ “By applying Lemma 1, we obtain ...” (**dependsOn**)
- ▶ “Theorem 2 provides an explicit algorithm ...” (**refersTo**)



Recognizing Navigational Relations

Supervised method

- 1 Given a segment S ; split its text into sentences, tokenize and do POS tagging
- 2 **Referential sentences** are ones that contain the `\ref` command entries
- 3 For each sentence:
 - find mentioned segments; each of them makes a pair with S (**type feature**)
 - for each pair, compute relative positions of segments normalized by the document size (**distance feature**)
 - build a boolean vector for its verbs (**verb feature**)



Recognizing Navigational Relations (cont.)

Supervised method

Example training instance

t1	t2	d1	d2	add	...	apply	...	relation
proof	lemma	0.09	0.27	0	...	1	...	dependsOn

- ▶ Train a learning model using these features and a labeled example set
- ▶ Apply the model to classify new induced relations



Recognizing Restricted Relations

The *hasConsequence*, *exemplifies* and *proves* relations are **restricted**

Assumption

Restricted relations occur between consecutive segments



Recognizing Restricted Relations (cont.)

Baseline method

According to the ontology, restricted relations involve instances of three types, separately: *Corollary*, *Example* and *Proof*

- 1 Seek a segment of one of these types
- 2 Find its segments-predecessors
- 3 Filter out segments of inappropriate types
- 4 Return the **closest predecessor**



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Experimental Setup

Collections

- ▶ 1355 papers of the “Izvestiya Vysshikh Uchebnykh Zavedenii. Matematika” journal
- ▶ A sample of 1031 papers from arXiv.org

Implementation

An open source **Java library** built upon:

- ▶ LaTeX-to-XML converters
- ▶ GATE framework
- ▶ Weka
- ▶ Jena

See <http://code.google.com/p/mocassin>

Segment Recognition Evaluation

- ▶ Evaluation on the arXiv sample only
- ▶ Q-gram string matching algorithm was used
- ▶ The threshold value was optimized w.r.t. F_1 -score

Type	# of true instances	F_1 -score
Axiom	5	1.000
Claim	114	0.987
Conjecture	152	0.987
Corollary	1715	0.995
Definition	1838	1.000
Example	771	0.999
Lemma	4061	0.998
Proof	4943	0.997
Proposition	3052	0.999
Remark	2114	1.000
Theorem	4670	0.991
<i>other</i>	671	0.892

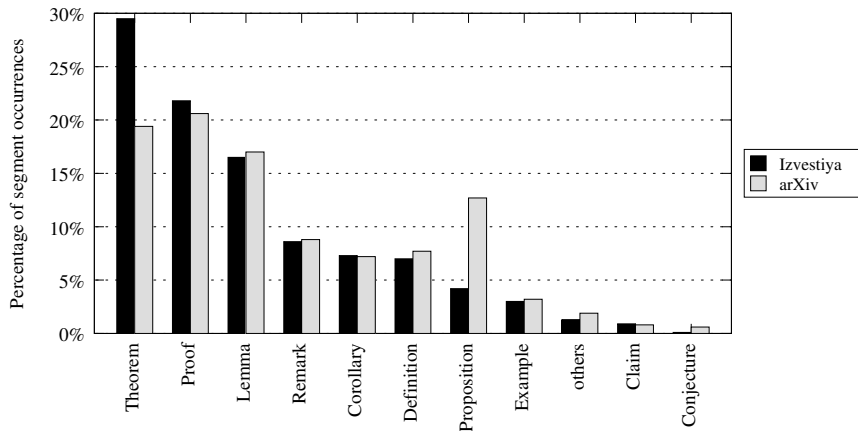


Ontology Coverage Evaluation

- ▶ Evaluation on the both entire collections (“Izvestiya” and arXiv)
- ▶ **Equations** are most ubiquitous segments (52% and 69%, respectively)
- ▶ The **ontology** covers types of 91.9% and 91.6% of segments (with SALT Section class – 99.5% and 99.6%)



Distribution of Segment Types



Evaluation of Navigational Relation Recognition

- ▶ A paper contains 51.4 ([Izvestiya](#)) and 53.9 ([arXiv](#)) referential sentences on the average
- ▶ 243 referential sentences were randomly selected and manually annotated
- ▶ 95% were true navigational relations
- ▶ A decision tree learner (C4.5) was trained
- ▶ The results were from 10-fold cross validation

Features	Accuracy	F_1 -score refersTo	F_1 -score dependsOn
type	0.663	0.566	0.752
type+distance	0.658	0.663	0.704
type+verb	0.704	0.653	0.770
type + distance + verb	0.741	0.744	0.772



Evaluation of Restricted Relation Recognition

- ▶ Evaluation on the arXiv sample only
- ▶ 10% of the documents which contain certain segments were randomly selected
- ▶ For each such a segment, corresponding relations were annotated manually
- ▶ Known issues: imported corollaries and examples for arbitrary text fragments

Relation	# of instances	F_1-score
hasConsequence	178	0.687
exemplifies	62	0.613
proves	216	0.954



Conclusion on Evaluation

- ▶ The **ontology** covers the largest part of the logical structure and appears to be feasible for **automatic extraction methods**
- ▶ The task of segment type recognition has been **accomplished**
- ▶ The method for recognizing navigational relations establishes **ground truth**, however, a large-scale evaluation and learning model selection are required
- ▶ The baseline method for recognizing restricted relations must be improved by leveraging additional information (**discussed in the paper!**)



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Prototype

A prototype:

- ▶ demonstrates our **ongoing research** on semantic search of mathematical papers
- ▶ incorporates the logical structure analysis methods
- ▶ is integrated with **arXiv API**
- ▶ enables **enhanced search** for arXiv papers and **visualization** of their logical structure
- ▶ publishes the semantic index as Linked Data via SPARQL endpoint



Search Interface

<http://cll.niimm.ksu.ru/mocassin>

Moca ∫∫ in

Find

turn inference on

$e = \lim_{n \rightarrow \infty} \left(1 + \frac{1}{n}\right)$ $e = \lim_{n \rightarrow \infty} \left(1 + \frac{1}{n}\right)$ $e = \lim_{n \rightarrow \infty} \left(1 + \frac{1}{n}\right)$

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Feedback



Formulating a Query

<http://cll.niimm.ksu.ru/mocassin>

Moca ∫∫ in

Find +

 +

- depends on
- has consequence
- has part
- has start page number
- has text
- has title
- refers to



Search Results

<http://cll.niimm.ksu.ru/mocassin>

Moca ∫∫ in

Find +
 +
 +
 +
 +

turn inference on

Results: 1

[A strengthening of the Nyman-Beurling criterion for the Riemann hypothesis, 2 \(Proof\)](#)
Luiz Duarte [\[arXiv\]](#) [\[RDF\]](#)

$$e = \lim_{n \rightarrow \infty} \left(1 + \frac{1}{n}\right)$$

$$e = \lim_{n \rightarrow \infty} \left(1 + \frac{1}{n}\right)$$

$$e = \frac{1+n}{n(1+n)} \sqrt{\frac{2}{5n}}$$

$$Ax = \lambda x$$

$$e = \frac{1+n}{n(1+n)} \sqrt{\frac{2}{5n}}$$



Preview a Search Result

<http://cll.niimm.ksu.ru/mocassin>

ON NYMAN-BEURLING CRITERION 7

Proof. We shall only sketch the proof of this proposition. Applying the Fourier-Mellin map (2.9) to $f_{\epsilon, n} + \chi$ we have from Plancherel's theorem that

$$\begin{aligned} 2\pi \|f_{\epsilon, n} + \chi\|_{\mathbb{R}}^2 &= \int_{\Re(s)=1/2} \left| \zeta(z) \sum_{a=1}^n \frac{\mu(a)}{a^{z+\epsilon}} - 1 \right|^2 \frac{|dz|}{|z|^2} \\ &\leq 2 \int_{\Re(s)=1/2} \left| \zeta(z) \left(\sum_{a=1}^n \frac{\mu(a)}{a^{z+\epsilon}} - \frac{1}{\zeta(z+\epsilon)} \right) \right|^2 \frac{|dz|}{|z|^2} \\ &\quad + 2 \int_{\Re(s)=1/2} \left| \frac{\zeta(z)}{\zeta(z+\epsilon)} - 1 \right|^2 \frac{|dz|}{|z|^2}. \end{aligned}$$

The second integral on the right-hand side above is estimated to be $\ll \epsilon^{2/3}$ as follows. If the distance between $z = \frac{1}{2} + it$ and the nearest zero of ζ is larger than δ , say, the upper bound

$$\left| \frac{\zeta(z)}{\zeta(z+\epsilon)} - 1 \right| \ll \epsilon \delta^{-1} (|t| + 1)^{3/4}$$

follows from the classical estimate

$$\frac{\zeta'(s)}{\zeta(s)} = \sum_{|r| \leq 1} \frac{1}{s-r} + O(\log(2+|r|)),$$

where $s = \sigma + ir$, $1/2 \leq \sigma \leq 3/4$, $r \in \mathbb{R}$ and $\rho = \beta + i\gamma$ denotes a generic zero of the ζ function, by integration and exponentiation, provided ϵ/δ is small enough. In the other case, one uses an estimate of Burnol [8] stating that under the Riemann hypothesis

Metadata

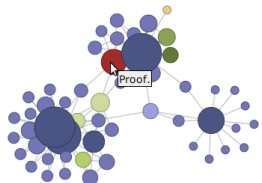
arXiv:

A strengthening of the Nyman-Beurling criterion for the hypothesis, 2

[Luiz Duarte](#)

Logical Structure Graph

hasPart refersTo dependsOn





Summary

- ▶ The proposed approach aims to analyze the structure of mathematical scholarly papers in an **automatic way**
- ▶ Our ontology provides a **controlled vocabulary** for analysis
- ▶ The methods elicit **document segments** in terms of the ontology
- ▶ The **extracted semantic graph** can be used for:
 - discovering important document parts
 - semantic search of theoretical results



Thanks for your attention!
Questions?

